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Pascal's Wager

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“Pascal's Wager” is the name given to an argument due to Blaise Pascal for believing, or for at least taking steps to believe, in God. The name is somewhat misleading, for in a single paragraph of his *Pensées*, Pascal apparently presents at least *three* such arguments, each of which might be called a ‘wager’ — it is only the final of these that is traditionally referred to as “Pascal's Wager”. We find in it the extraordinary confluence of several important strands of thought: the justification of theism; probability theory and decision theory, used here for almost the first time in history; pragmatism; voluntarism (the thesis that belief is a matter of the will); and the use of the concept of infinity.

We will begin with some brief stage-setting: some historical background, some of the basics of decision theory, and some of the exegetical problems that the *Pensées* pose. Then we will follow the text to extract three main arguments. The bulk of the literature addresses the third of these arguments, as will the bulk of our discussion here. Some of the more technical and scholarly aspects of our discussion will be relegated to lengthy footnotes, to which there are links for the interested reader. All quotations are from §233 of *Pensées* (1910, Trotter translation), the ‘thought’ whose heading is “*Infinite—nothing*”.

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1. Background

It is important to contrast Pascal's argument with various putative ‘proofs’ of the existence of God that had come before it. Anselm's ontological argument, Aquinas' ‘five ways’, Descartes' ontological and cosmological arguments, and so on, purport to

prove that God exists. Pascal is apparently unimpressed by such attempted justifications of theism: “Endeavour ... to convince yourself, not by increase of proofs of God...” Indeed, he concedes that “we do not know if He is ...”. Pascal's project, then, is radically different: he seeks to provide *prudential* reasons for believing in God. To put it crudely, we should wager that God exists because it is the *best bet*. Ryan 1994 finds precursors to this line of reasoning in the writings of Plato, Arnobius, Lactantius, and others; we might add Ghazali to his list — see Palacios 1920. But what is distinctive is Pascal's explicitly decision theoretic formulation of the reasoning. In fact, Hacking 1975 describes the Wager as “the first well-understood contribution to decision theory” (viii). Thus, we should pause briefly to review some of the basics of that theory.

In any decision problem, the way the world is, and what an agent does, together determine an outcome for the agent. We may assign *utilities* to such outcomes, numbers that represent the degree to which the agent values them. It is typical to present these numbers in a decision matrix, with the columns corresponding to the various relevant states of the world, and the rows corresponding to the various possible actions that the agent can perform.

In *decisions under uncertainty*, nothing more is given — in particular, the agent does not assign subjective probabilities to the states of the world. Still, sometimes rationality dictates a unique decision nonetheless. Consider, for example, a case that will be particularly relevant here. Suppose that you have two possible actions, A1 and A2, and the worst outcome associated with A1 is at least as good as the best outcome associated with A2; suppose also that in at least one state of the world, A1's outcome is strictly better than A2's. Let us say in that case that A1 *superdominates* A2. Then rationality seems to require you to perform A1.^[1]

In *decisions under risk*, the agent assigns subjective probabilities to the various states of the world. Assume that the states of the world are independent of what the agent does. A figure of merit called the *expected utility*, or the *expectation* of a given action can be calculated by a simple formula: for each state, multiply the utility that the action produces in that state by the state's probability; then, add these numbers. According to decision theory, rationality requires you to perform the action of maximum expected utility (if there is one).

Example. Suppose that the utility of money is linear in number of dollars: you value money at exactly its face value. Suppose that you have the option of paying a dollar to play a game in which there is an equal chance of returning nothing, and returning three dollars. The expectation of the game itself is

$$0 \times (1/2) + 3 \times (1/2) = 1.5,$$

so the expectation of paying a dollar for certain, then playing, is

$$-1 + 1.5 = 0.5.$$

This exceeds the expectation of not playing (namely 0), so you should play. On the

other hand, if the game gave an equal chance of returning nothing, and returning two dollars, then its expectation would be:

$$0 \times (1/2) + 2 \times (1/2) = 1.$$

Then consistent with decision theory, you could either pay the dollar to play, or refuse to play, for either way your overall expectation would be 0.

Considerations such as these will play a crucial role in Pascal's arguments. It should be admitted that there are certain exegetical problems in presenting these arguments. Pascal never finished the *Pensées*, but rather left them in the form of notes of various sizes pinned together. Hacking 1972 describes the “Infinite—nothing” as consisting of “two pieces of paper covered on both sides by handwriting going in all directions, full of erasures, corrections, insertions, and afterthoughts” (24).^[2] This may explain why certain passages are notoriously difficult to interpret, as we will see. Furthermore, our formulation of the arguments in the parlance of modern Bayesian decision theory might appear somewhat anachronistic. For example, Pascal did not distinguish between what we would now call *objective* and *subjective* probability, although it is clear that it is the latter that is relevant to his arguments. To some extent, “Pascal's Wager” now has a life of its own, and our presentation of it here is perfectly standard. Still, we will closely follow Pascal's text, supporting our reading of his arguments as much as possible.

There is the further problem of dividing the *Infinite-nothing* into separate arguments. We will locate three arguments that each conclude that rationality requires you to wager for God, although they interleave in the text.^[3] Finally, there is some disagreement over just what “wagering for God” involves — is it *believing* in God, or merely *trying* to? We will conclude with a discussion of what Pascal meant by this.

2. The Argument from Superdominance

Pascal maintains that we are incapable of knowing whether God exists or not, yet we must “wager” one way or the other. Reason cannot settle which way we should incline, but a consideration of the relevant outcomes supposedly can. Here is the first key passage:

“God is, or He is not.” But to which side shall we incline? Reason can decide nothing here. There is an infinite chaos which separated us. A game is being played at the extremity of this infinite distance where heads or tails will turn up... Which will you choose then? Let us see. Since you must choose, let us see which interests you least. You have two things to lose, the true and the good; and two things to stake, your reason and your will, your knowledge and your happiness; and your nature has two things to shun, error and misery. Your reason is no more shocked in choosing one rather than the other, since you must of necessity choose... But your happiness? Let us weigh the gain and the loss in wagering that God is... If you gain, you gain all; if you lose, you lose nothing. Wager, then, without hesitation that He is.

There are exegetical problems already here, partly because Pascal appears to contradict himself. He speaks of “the true” as something that you can “lose”, and “error” as something “to shun”. Yet he goes on to claim that if you lose the wager that God is, then “you lose nothing”. Surely in that case you “lose the true”, which is just to say that you have made an error. Pascal believes, of course, that the existence of God is “the true” — but *that* is not something that he can appeal to in this argument. Moreover, it is not because “you must of necessity choose” that “your reason is no more shocked in choosing one rather than the other”. Rather, by Pascal's own account, it is because “[r]eason can decide nothing here”. (If it could, then it might well be shocked — namely, if you chose in a way contrary to it.)

Following McClennen 1994, Pascal's argument seems to be best captured as presenting the following decision matrix:

	<i>God exists</i>	<i>God does not exist</i>
<i>Wager for God</i>	Gain all	Status quo
<i>Wager against God</i>	Misery	Status quo

Wagering for God superdominates wagering against God: the worst outcome associated with wagering for God (status quo) is at least as good as the best outcome associated with wagering against God (status quo); and if God exists, the result of wagering for God is strictly better than the result of wagering against God. (The fact that the result is *much* better does not matter yet.) Pascal draws the conclusion at this point that rationality requires you to wager for God.

Without any assumption about your probability assignment to God's existence, the argument is invalid. Rationality does *not* require you to wager for God if you assign probability 0 to God existing. And Pascal does not explicitly rule this possibility out until a later passage, when he assumes that you assign positive probability to God's existence; yet this argument is presented as if it is self-contained. His claim that “[r]eason can decide nothing here” may suggest that Pascal regards this as a decision under uncertainty, which is to assume that you do *not* assign probability at all to God's existence. If that is a further premise, then the argument is apparently valid; but that premise contradicts his subsequent assumption that you assign positive probability. See McClennen for a reading of this argument as a decision under uncertainty.

Pascal appears to be aware of a further objection to this argument, for he immediately imagines an opponent replying:

“That is very fine. Yes, I must wager; but I may perhaps wager too much.”

The thought seems to be that if I wager for God, and God does not exist, then I really do lose something. In fact, Pascal himself speaks of *staking something* when one wagers for God, which presumably one loses if God does not exist. (We have already mentioned ‘the true’ as one such thing; Pascal also seems to regard one's worldly life as another.) In other words, the matrix is mistaken in presenting the two outcomes

under ‘God does not exist’ as if they were the same, and we do not have a case of superdominance after all.

Pascal addresses this at once in his second argument, which we will discuss only briefly, as it can be thought of as just a prelude to the main argument.

3. The Argument From Expectation

He continues:

Let us see. Since there is an equal risk of gain and of loss, if you had only to gain two lives, instead of one, you might still wager. But if there were three lives to gain, you would have to play (since you are under the necessity of playing), and you would be imprudent, when you are forced to play, not to chance your life to gain three at a game where there is an equal risk of loss and gain. But there is an eternity of life and happiness.

His hypothetically speaking of “two lives” and “three lives” may strike one as odd. It is helpful to bear in mind Pascal's interest in gambling (which after all provided the initial motivation for his study of probability) and to take the gambling model quite seriously here. Indeed, the Wager is permeated with gambling metaphors: “game”, “stake”, “heads or tails”, “cards” and, of course, “wager”. Now, recall our calculation of the expectations of the two dollar and three dollar gambles. Pascal apparently assumes now that utility is linear in number of *lives*, that wagering for God costs “one life”, and then reasons analogously to the way we did! This is, as it were, a warm-up. Since wagering for God is rationally required even in the hypothetical case in which one of the prizes is three lives, then all the more it is rationally required in the actual case, in which one of the prizes is an *eternity* of life (salvation).

So Pascal has now made two striking assumptions:

- (1) The probability of God's existence is $1/2$.
- (2) Wagering for God brings *infinite* reward if God exists.

Morris 1994 is sympathetic to (1), while Hacking 1972 finds it “a monstrous premiss”. One way to defend it is via the classical interpretation of probability, according to which all possibilities are given equal weight. To be sure, unless more is said, the interpretation yields implausible, and even contradictory results. (You have a one-in-a-million chance of winning the lottery; but either you win the lottery or you don't, so each of these possibilities has probability $1/2$?!). Pascal's argument for (1) is presumably that “[r]eason can decide nothing here”. (In the lottery ticket case, reason can decide *something*.) But it is not clear that complete ignorance should be modeled as sharp indifference. Morris imagines, rather, an agent who does have evidence for and against the existence of God, but it is equally balanced. In any case, it *is* clear that there are people in Pascal's audience who do not assign probability $1/2$ to God's existence. This argument, then, does not speak to them.

However, Pascal realizes that the value of $1/2$ actually plays no real role in the

argument, thanks to (2). This brings us to the third, and by far the most important, of his arguments.

4. The Argument From Generalized Expectations: “Pascal's Wager”

We continue the quotation.

But there is an eternity of life and happiness. And this being so, if there were an infinity of chances, of which one only would be for you, you would still be right in wagering one to win two, and you would act stupidly, being obliged to play, by refusing to stake one life against three at a game in which out of an infinity of chances there is one for you, if there were an infinity of an infinitely happy life to gain. But there is here an infinity of an infinitely happy life to gain, a chance of gain against a finite number of chances of loss, and what you stake is finite. It is all divided; wherever the infinite is and there is not an infinity of chances of loss against that of gain, there is no time to hesitate, you must give all...

Again this passage is difficult to understand completely. Pascal's talk of winning two, or three, lives is a little misleading. By his own decision theoretic lights, you would *not* act stupidly “by refusing to stake one life against three at a game in which out of an infinity of chances there is one for you”—in fact, you should not stake more than an infinitesimal amount in that case (an amount that is bigger than 0, but smaller than every positive real number). The point, rather, is that the prospective prize is “an infinity of an infinitely happy life”. In short, if God exists, then wagering for God results in infinite utility.

What about the utilities for the other possible outcomes? There is some dispute over the utility of “misery”. Hacking interprets this as “damnation”, and Pascal does later speak of “hell” as the outcome in this case. Martin 1983 among others assigns this a value of *negative infinity*. Sobel 1996, on the other hand, is one author who takes this value to be finite. There is some textual support for this reading: “The justice of God must be vast like His compassion. Now justice to the outcast is less vast ... than mercy towards the elect”. As for the utilities of the outcomes associated with God's non-existence, Pascal tells us that “what you stake is finite”. This suggests that whatever these values are, they are finite.

Pascal's guiding insight is that the argument from expectation goes through equally well *whatever* your probability for God's existence is, provided that it is non-zero and finite (non-infinitesimal) — “a chance of gain against a finite number of chances of loss”.^[4]

With Pascal's assumptions about utilities and probabilities in place, he is now in a position to calculate the relevant expectations. He explains how the calculations should proceed:

... the uncertainty of the gain is proportioned to the certainty of the stake

according to the proportion of the chances of gain and loss... ^[5]

Let us now gather together all of these points into a single argument. We can think of Pascal's Wager as having three premises: the first concerns the decision matrix of rewards, the second concerns the probability that you should give to God's existence, and the third is a maxim about rational decision-making. Specifically:

1. Either God exists or God does not exist, and you can either wager for God or wager against God. The utilities of the relevant possible outcomes are as follows, where f_1 , f_2 , and f_3 are numbers whose values are not specified beyond the requirement that they be finite:

	<i>God exists</i>	<i>God does not exist</i>
<i>Wager for God</i>	∞	f_1
<i>Wager against God</i>	f_2	f_3

2. Rationality requires the probability that you assign to God existing to be positive, and not infinitesimal.
3. Rationality requires you to perform the act of maximum expected utility (when there is one).
4. Conclusion 1. Rationality requires you to wager for God.
5. Conclusion 2. You should wager for God.

We have a decision under risk, with probabilities assigned to the relevant ways the world could be, and utilities assigned to the relevant outcomes. The first conclusion seems straightforwardly to follow from the usual calculations of expected utility (where p is your positive, non-infinitesimal probability for God's existence):

$$E(\text{wager for God}) = \infty \times p + f_1 \times (1 - p) = \infty$$

That is, your expected utility of belief in God is infinite — as Pascal puts it, “our proposition is of infinite force”. On the other hand, your expected utility of wagering against God is

$$E(\text{wager against God}) = f_2 \times p + f_3 \times (1 - p)$$

This is finite.^[6] By premise 3, rationality requires you to perform the act of maximum expected utility. Therefore, rationality requires you to wager for God.

We now survey some of the main objections to the argument.

5. Objections to Pascal's Wager

Premise 1: The Decision Matrix

Here the objections are manifold. Most of them can be stated quickly, but we will give special attention to what has generally been regarded as the most important of them, ‘the many Gods objection’ (see also the link to footnote 7).

1. Different matrices for different people. The argument assumes that the same decision matrix applies to everybody. However, perhaps the relevant rewards are different for different people. Perhaps, for example, there is a predestined infinite reward for the Chosen, whatever they do, and finite utility for the rest, as Mackie 1982 suggests. Or maybe the prospect of salvation appeals more to some people than to others, as Swinburne 1969 has noted.

Even granting that a single 2×2 matrix applies to everybody, one might dispute the values that enter into it. This brings us to the next two objections.

2. The utility of salvation could not be infinite. One might argue that the very notion of infinite utility is suspect — see for example Jeffrey 1983 and McClennen 1994.^[7] Hence, the objection continues, whatever the utility of salvation might be, it must be finite. Strict finitists, who are chary of the notion of infinity in general, will agree — see Dummett 1978 and Wright 1987. Or perhaps the notion of infinite utility makes sense, but an infinite reward could only be finitely appreciated by a human being.

3. There should be more than one infinity in the matrix. There are also critics of the Wager who, far from objecting to infinite utilities, want to see *more* of them in the matrix. For example, it might be thought that a forgiving God would bestow infinite utility upon wagerers-for and wagerers-against alike — Rescher 1985 is one author who entertains this possibility. Or it might be thought that, on the contrary, wagering against an existent God results in *negative* infinite utility. (As we have noted, some authors read Pascal himself as saying as much.) Either way, f_2 is not really finite at all, but ∞ or $-\infty$ as the case may be. And perhaps f_1 and f_3 could be ∞ or $-\infty$. Suppose, for instance, that God does not exist, but that we are reincarnated *ad infinitum*, and that the total utility we receive is an infinite sum that diverges to infinity or to negative infinity.

4. The matrix should have more rows. Perhaps there is more than one way to wager for God, and the rewards that God bestows vary accordingly. For instance, God might not reward infinitely those who strive to believe in Him only for the very mercenary reasons that Pascal gives, as James 1956 has observed. One could also imagine distinguishing belief based on faith from belief based on evidential reasons, and posit different rewards in each case.

5. The matrix should have more columns: the many Gods objection. If Pascal is really right that reason can decide nothing here, then it would seem that various other theistic hypotheses are also live options. Pascal presumably had in mind the Catholic conception of God — let us suppose that this is the God who either ‘exists’ or ‘does not exist’. By excluded middle, this is a partition. The objection, then, is that the partition is not sufficiently fine-grained, and the ‘(Catholic) God does not exist’ column really subdivides into various *other* theistic hypotheses. The objection could equally run that Pascal's argument ‘proves too much’: by parallel reasoning we can ‘show’ that rationality requires believing in various incompatible theistic hypotheses. As Diderot (1746) puts the point: “An Imam could reason just as well this way”.^[8]

Since then, the point has been presented again and refined in various ways. Mackie

1982 writes, “the church within which alone salvation is to be found is not necessarily the Church of Rome, but perhaps that of the Anabaptists or the Mormons or the Muslim Sunnis or the worshippers of Kali or of Odin” (203). Cargile 1966 shows just how easy it is to multiply theistic hypotheses: for each real number x , consider the God who prefers contemplating x more than any other activity. It seems, then, that such ‘alternative gods’ are a dime a dozen — or aleph one, for that matter.

In response, some authors argue that in such a competition among various possible deities for one's belief, some are more probable than others. Although there may be ties among the expected utilities — all infinite — for believing in various ones among them, their respective probabilities can be used as tie-breakers. Schlesinger (1994) offers this principle: “In cases where the mathematical expectations are infinite, the criterion for choosing the outcome to bet on is its probability” (90). (Note that this principle is not found in the Wager itself, although it might be regarded as a friendly addition.) Are there reasons, then, for assigning higher probability to some Gods than others? Jordan (1994a, 107) suggests that some outlandish theistic hypotheses may be dismissed for having “no backing of tradition”. Similarly, Schlesinger maintains that Pascal is addressing readers who “have a notion of what genuine religion is about” (88), and we might take that to suggest that Cargile's imagined Gods, for example, may be correspondingly assigned lower probability than Pascal's God. Lycan and Schlesinger (1989) give more theoretical reasons for favoring Pascal's God over others in one's probability assignments. They begin by noting the familiar problem in science of underdetermination of theory by evidence. Faced with a multiplicity of theories that all fit the observed data equally well, we favor the simplest such theory. They go on to argue that simplicity considerations similarly favor a conception of God as “absolutely perfect”, “which is theologically unique in that it implies all the other predicates traditionally ascribed to God” (104), and we may add that this conception is Pascal's. Conceptions of rival Gods, by contrast, leave open various questions about their nature, the answering of which would detract from their simplicity, and thus their probability.

Finally, Bartha (2012) models one's probability assignments to various theistic hypotheses as evolving over time according to a ‘deliberational dynamics’ somewhat analogous to the dynamics of evolution by natural selection. So understood, Pascal's Wager is not a single decision, but rather a sequence of decisions in which one's probabilities update sequentially in proportion to how choiceworthy each God appeared to be in the previous round. (This relies on a sophisticated handling of infinite utilities in terms of utility ratios given in his (2007); see below.) He argues that a given probability assignment is choiceworthy only if it is an equilibrium of this deliberational dynamics. He shows that certain assignments are choiceworthy by this criterion, thus providing a kind of vindication of Pascal against the many Gods objection.

Premise 2: The Probability Assigned to God's Existence

There are four sorts of problem for this premise. The first two are straightforward; the second two are more technical, and can be found by following the link to footnote 8.

1. Undefined probability for God's existence. Premise 1 presupposes that you should *have* a probability for God's existence in the first place. However, perhaps you could rationally *fail* to assign it a probability — your probability that God exists could remain *undefined*. We cannot enter here into the thorny issues concerning the attribution of probabilities to agents. But there is some support for this response even in Pascal's own text, again at the pivotal claim that “[r]eason can decide nothing here. There is an infinite chaos which separated us. A game is being played at the extremity of this infinite distance where heads or tails will turn up...” The thought could be that any probability assignment is inconsistent with a state of “epistemic nullity” (in Morris' 1986 phrase): to assign a probability at all — even 1/2 — to God's existence is to feign having evidence that one in fact totally lacks. For unlike a coin that we know to be fair, this metaphorical ‘coin’ is ‘infinitely far’ from us, hence apparently completely unknown to us. Perhaps, then, rationality actually requires us to *refrain* from assigning a probability to God's existence (in which case at least the Argument from Superdominance would apparently be valid). Or perhaps rationality does not require it, but at least *permits* it. Either way, the Wager would not even get off the ground.

2. Zero probability for God's existence. Strict atheists may insist on the rationality of a probability assignment of 0, as Oppy 1990 among others points out. For example, they may contend that reason alone *can* settle that God does not exist, perhaps by arguing that the very notion of an omniscient, omnipotent, omnibenevolent being is contradictory. Or a Bayesian might hold that rationality places no constraint on probabilistic judgments beyond coherence (or conformity to the probability calculus). Then as long as the strict atheist assigns probability 1 to God's non-existence alongside his or her assignment of 0 to God's existence, no norm of rationality has been violated.

Furthermore, an assignment of $p = 0$ would clearly block the route to Pascal's conclusion. For then the expectation calculations become:

$$E(\text{wager for God}) = \infty \times 0 + f_1 \times (1 - 0) = f_1$$

$$E(\text{wager against God}) = f_2 \times 0 + f_3 \times (1 - 0) = f_3$$

And nothing in the argument implies that $f_1 > f_3$. (Indeed, this inequality is questionable, as even Pascal seems to allow.) In short, Pascal's wager has no pull on strict atheists.^[9]

Premise 3: Rationality Requires Maximizing Expected Utility

Finally, one could question Pascal's decision theoretic assumption that rationality requires one to perform the act of maximum expected utility (when there is one). Now *perhaps* this is an analytic truth, in which case we could grant it to Pascal without further discussion — perhaps it is *constitutive* of rationality to maximize expectation, as some might say. But this premise has met serious objections. The Allais 1953 and Ellsberg 1961 paradoxes, for example, are said to show that maximizing expectation can lead one to perform intuitively sub-optimal actions. So too the St. Petersburg paradox, in which it is supposedly absurd that one should be prepared to pay any finite amount to play a game with infinite expectation. (That

paradox is particularly apposite here.)^[10]

Various refinements of expected utility theory have been suggested as a result of such problems. For example, we might consider expected *differences* between the pay-offs of options, and prefer one option to another if and only if the expected difference of the former relative to the latter is positive — see Hájek and Nover 2006, Hájek 2006, and Colyvan 2008. Or we might consider suitably defined utility *ratios*, and prefer one option to another if and only if the utility ratio of the former relative to the latter is greater than 1 — see Bartha 2007. If we either admit refinements of traditional expected utility theory, or are pluralistic about our decision rules, then premise 3 is apparently false as it stands. Nonetheless, the door is opened to some suitable reformulation of it that might serve Pascal's purposes. Indeed, Bartha argues that his ratio-based reformulation answers some of the most pressing objections to the Wager that turn on its invocation of infinite utility.

Finally, one might distinguish between *practical* rationality and *theoretical* rationality. One could then concede that practical rationality requires you to maximize expected utility, while insisting that theoretical rationality might require something else of you — say, proportioning belief to the amount of evidence available. This objection is especially relevant, since Pascal admits that perhaps you “must renounce reason” in order to follow his advice. But when these two sides of rationality pull in opposite directions, as they apparently can here, it is not obvious that practical rationality should take precedence. (For a discussion of pragmatic, as opposed to theoretical, reasons for belief, see Foley 1994.)

Is the Argument Valid?

A number of authors who have been otherwise critical of the Wager have explicitly conceded that the Wager is valid — e.g. Mackie 1982, Rescher 1985, Mougin and Sober 1994, and most emphatically, Hacking 1972. That is, these authors agree with Pascal that wagering for God really is rationally mandated by Pascal's decision matrix in tandem with positive probability for God's existence, and the decision theoretic account of rational action.

However, Duff 1986 and Hájek 2003 argue that the argument is in fact invalid. Their point is that there are strategies besides wagering for God that also have infinite expectation — namely, *mixed* strategies, whereby you do not wager for or against God outright, but rather choose which of these actions to perform on the basis of the outcome of some chance device. Consider the mixed strategy: “Toss a fair coin: heads, you wager for God; tails, you wager against God”. By Pascal's lights, with probability 1/2 your expectation will be infinite, and with probability 1/2 it will be finite. The expectation of the entire strategy is:

$$1/2 \times \infty + 1/2[f_2 \times p + f_3 \times (1 - p)] = \infty$$

That is, the ‘coin toss’ strategy has the same expectation as outright wagering for God. But the probability 1/2 was incidental to the result. Any mixed strategy that gives positive and finite probability to wagering for God will likewise have infinite

expectation: “wager for God iff a fair die lands 6”, “wager for God iff your lottery ticket wins”, “wager for God iff a meteor quantum tunnels its way through the side of your house”, and so on.

It can be argued that the problem is still worse than this, though, for there is a sense in which *anything* that you do might be regarded as a mixed strategy between wagering for God, and wagering against God, with suitable probability weights given to each. Suppose that you choose to ignore the Wager, and to go and have a hamburger instead. Still, you may well assign positive and finite probability to your winding up wagering for God nonetheless; and this probability multiplied by infinity again gives infinity. So ignoring the Wager and having a hamburger has the same expectation as outright wagering for God. Even worse, suppose that you focus all your energy into *avoiding* belief in God. Still, you may well assign positive and finite probability to your efforts failing, with the result that you wager for God nonetheless. In that case again, your expectation is infinite again. So even if rationality requires you to perform the act of maximum expected utility when there is one, here there isn't one. Rather, there is a many-way tie for first place, as it were. All hell breaks loose: anything you might do is maximally good!^[11]

Monton (2011) defends Pascal's Wager against this line of objection. He argues that an atheist or agnostic has more than one opportunity to follow a mixed strategy. Returning to the first example of one, suppose that the fair coin lands tails. Monton's thought is that your expected utility now changes; it is no longer infinite, but rather that of an atheist or agnostic who has no prospect of the infinite reward for wagering for God. You are back to where you started. But since it was rational for you to follow the mixed strategy the first time, it is rational for you to follow it again now—that is, to toss the coin again. And if it lands tails again, it is rational for you to toss the coin again ... With probability 1, the coin will land heads eventually, and from that point on you will wager for God. Similar reasoning applies to wagering for God just in case an n -sided die lands 1 (say): with probability 1 the die will eventually land 1, so if you repeatedly base your mixed strategy on the die, with probability 1 you will wind up wagering for God after a finite number of rolls. Robertson (2012) replies that not all such mixed strategies are (probabilistically) guaranteed to lead to your wagering for God in the long run: not ones in which the probability of wagering for God decreases sufficiently fast on successive trials. Think, for example, of rolling a 4-sided die, then a 9-sided die, and in general an $(n+1)^2$ -sided die on the n^{th} trial ..., a strategy for which the probability that you will eventually wager for God is only $1/2$, as Robertson shows. However, Easwaran and Monton (2012) counter-reply that with a continuum of times at which the dice can be rolled, the sequence of rolls that Robertson proposes can be completed in an arbitrarily short period of time. In that case, what should you do next? By Monton's argument, it seems you should roll a die again. Easwaran and Monton prove that if there are uncountably many times at which one implements a mixed strategy with non-zero probability of wagering for God, then with probability 1, one ends up wagering for God at one of these times. (And they assume, as is standard, that once one wagers for God there is no going back.) They concede that imagining uncountably rolls of a die, say, involves an idealization that is surely not physically realizable. But they maintain that you should act in the way that an idealized version

of yourself would eventually act, one who *can* realize the rolls as described—that is, wager for God outright.

There is a further twist on the mixed strategies objection. To repeat, the objection's upshot is that even granting Pascal all his premises, still wagering for God is not rationally required. But we have seen numerous reasons *not* to grant all his premises. Very well then; let's not. Indeed, let's suppose that you give *tiny probability* p to them all being true, where p is positive and finite. So you assign probability p to your decision problem being exactly as Pascal claims it to be. But if it is, according to the mixed strategies objection, all hell breaks loose. Yet again, p multiplied by infinity gives infinity. Hence, it seems that each action that gets infinite expected utility according to Pascal similarly gets infinite expected utility according to *you*; but by the previous reasoning, that is anything you might do. The full force of the objection that hit Pascal now hits you too. There are some subtleties that we have elided over; for example, if you also assign positive and finite probability to a source of *negative* infinite utility, then the expected utilities instead become $\infty - \infty$, which is undefined. But that is just another way for all hell to break loose for you: in that case, you cannot evaluate the choiceworthiness of your possible actions at all. Either way, you face decision-theoretic paralysis. We might call this *Pascal's Revenge*. See Hájek (forthcoming) for more discussion.

Moral Objections to Wagering for God

Let us grant Pascal's conclusion for the sake of the argument: rationality requires you to wager for God. It still does not obviously follow that you *should* wager for God. All that we have granted is that one norm — the norm of rationality — prescribes wagering for God. For all that has been said, some *other* norm might prescribe wagering against God. And unless we can show that the rationality norm trumps the others, we have not settled what we should actually do.

There are several arguments to the effect that *morality* requires you to wager against God. Pascal himself appears to be aware of one such argument. He admits that if you do not believe in God, his recommended course of action will “deaden your acuteness.” One way of putting the argument is that wagering for God may require you to corrupt yourself, thus violating a Kantian duty to yourself. Clifford 1877 argues that an individual's believing something on insufficient evidence harms society by promoting credulity. Penelhum 1971 contends that the putative divine plan is itself immoral, condemning as it does honest non-believers to loss of eternal happiness, when such unbelief is in no way culpable; and that to adopt the relevant belief is to be complicit to this immoral plan. See Quinn 1994 for replies to these arguments. For example, against Penelhum he argues that as long as God treats non-believers justly, there is nothing immoral about him bestowing special favor on believers, more perhaps than they deserve. (Note, however, that Pascal leaves open in the Wager whether the payoff for non-believers *is* just; indeed, as far as his argument goes, it may be extremely unjust.)

Finally, Voltaire protests that there is something unseemly about the whole Wager. He suggests that Pascal's calculations, and his appeal to self-interest, are unworthy of the

gravity of the subject of theistic belief. This does not so much support wagering against God, as dismissing all talk of ‘wagerings’ altogether. Schlesinger (1994, 84) canvasses a sharpened formulation of this objection: an appeal to greedy, self-interested motivations is incompatible with “the quest for piety” that is essential to religion. He replies that the pleasure of salvation that Pascal's Wager countenances is “of the most exalted kind”, and that if seeking it counts as greed at all, then it is “the manifestation of a noble greed that is to be acclaimed” (85).

What Does It Mean to “Wager for God”?

Let us now grant Pascal that, all things considered (rationality and morality included), you should wager for God. What exactly does this involve?

A number of authors read Pascal as arguing that you should *believe* in God — see e.g. Quinn 1994, and Jordan 1994a. But perhaps one cannot simply believe in God at will; and rationality cannot require the impossible. Pascal is well aware of this objection: “[I] am so made that I cannot believe. What, then, would you have me do?”, says his imaginary interlocutor. However, he contends that one can take steps to cultivate such belief:

You would like to attain faith, and do not know the way; you would like to cure yourself of unbelief, and ask the remedy for it. Learn of those who have been bound like you, and who now stake all their possessions. These are people who know the way which you would follow, and who are cured of an ill of which you would be cured. Follow the way by which they began; by acting as if they believed, taking the holy water, having masses said, etc. ...

But to show you that this leads you there, it is this which will lessen the passions, which are your stumbling-blocks.

We find two main pieces of advice to the non-believer here: act like a believer, and suppress those passions that are obstacles to becoming a believer. And these are actions that one *can* perform at will.

Believing in God is presumably one way to wager for God. This passage suggests that even the non-believer can wager for God, by striving to become a believer. Critics may question the psychology of belief formation that Pascal presupposes, pointing out that one could strive to believe (perhaps by following exactly Pascal's prescription), yet fail. To this, a follower of Pascal might reply that the act of genuine striving already displays a pureness of heart that God would fully reward; or even that genuine striving in this case is itself a form of believing.

According to Pascal, ‘wagering for God’ and ‘wagering against God’ are contradictories, as there is no avoiding wagering one way or another: “you must wager. It is not optional.” The decision to wager for or against God is one that you make at a time—at *t*, say. But of course Pascal does not think that you would be infinitely rewarded for wagering for God momentarily, then wagering against God

thereafter; nor that you would be infinitely rewarded for wagering for God sporadically—only on the last Thursday of each month, for example. What Pascal intends by ‘wagering for God’ is an ongoing action—indeed, one that continues until your death—that involves your adopting a certain set of practices and living the kind of life that fosters belief in God. The decision problem for you at t , then, is whether you should embark on this course of action; to fail to do so is to wager against God at t .

Pascal's Wager vies with Anselm's Ontological Argument for being the most famous argument in the philosophy of religion. As we have seen, it is a great deal more besides.

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